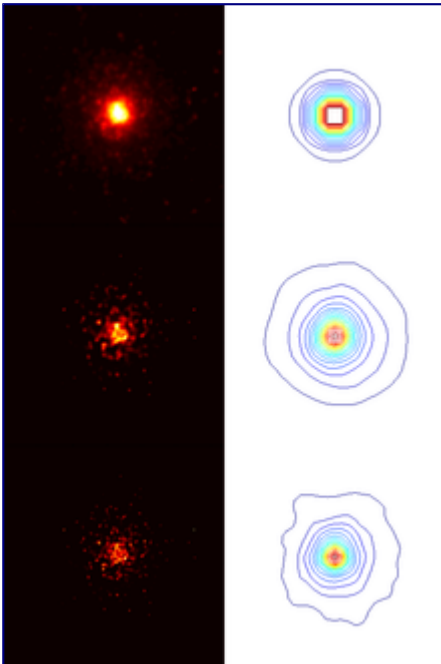


# Blind deconvolution

In electrical engineering and [applied mathematics](#), **blind deconvolution** refers to [deconvolution](#) without explicit knowledge of the [impulse response function](#) used in the [convolution](#). In microscopy the term is used to describe deconvolution without knowledge of the microscopes point spread function. This is usually achieved by making appropriate assumptions of the input to estimate the impulse response by analyzing the output.



Top left image: NGC224 by [Hubble Space Telescope](#). Top right contour: best fit of the [point spread function](#) (PSF) (a priori).<sup>[1]</sup> Middle left image: Deconvolution by [maximum a posteriori estimation](#) (MAP), the 2nd iteration. Middle right contour: Estimate of the PSF by MAP, the 2nd iteration. Bottom left image: Deconvolution by MAP, the final result. Bottom right contour: Estimate of the PSF by MAP, the final result.

## In image processing

In [image processing](#), blind deconvolution is a deconvolution technique that permits recovery of the target scene from a single or set of "blurred" images in the presence of a poorly determined or unknown [point spread function](#) (PSF).<sup>[2]</sup> Regular linear and non-linear deconvolution techniques utilize a known PSF. For blind deconvolution, the PSF is estimated from the image or image set, allowing the deconvolution to be performed. Researchers have been studying blind deconvolution methods for several decades, and have approached the problem from different directions.

Blind deconvolution can be performed iteratively, whereby each iteration improves the estimation of the PSF and the scene, or non-iteratively, where one application of the algorithm, based on exterior information, extracts the PSF. Iterative methods include [maximum a posteriori estimation](#) and [expectation-maximization algorithms](#). A good estimate of the PSF is helpful for quicker convergence but not necessary.

Examples of non-iterative techniques include SeDDaRA, the [cepstrum](#) transform and APEX. The

cepstrum transform and APEX methods assume that the PSF has a specific shape, and one must estimate the width of the shape. For SeDDaRA, the information about the scene is provided in the form of a reference image. The algorithm estimates the PSF by comparing the spatial frequency information in the blurred image to that of the target image.

## In signal processing

### Seismic data

In the case of [deconvolution of seismic data](#), the original unknown signal is made of spikes hence is possible to characterize with [sparsity](#) constraints[3] or [regularizations](#) such as  $l_1$  norm/ $l_2$  norm norm ratios,[4] suggested by W. C. Gray in 1978.[5]

### Audio deconvolution

Audio deconvolution (often referred to as *dereverberation*) is a [reverberation](#) reduction in audio mixtures. It is part of audio processing of recordings in ill-posed cases such as the [cocktail party effect](#). One possibility is to use [ICA](#). [6]

### In general

Suppose we have a signal transmitted through a channel. The channel can usually be modeled as a [linear shift-invariant system](#), so the receptor receives a convolution of the original signal with the impulse response of the channel. If we want to reverse the effect of the channel, to obtain the original signal, we must process the received signal by a second linear system, inverting the response of the channel. This system is called an [equalizer](#).

If we are given the original signal, we can use a supervising technique, such as finding a [Wiener filter](#), but without it, we can still explore what we do know about it to attempt its recovery. For example, we can filter the received signal to obtain the desired [spectral power density](#). This is what happens, for example, when the original signal is known to have no [auto correlation](#), and we "[whiten](#)" the received signal.

Whitening usually leaves some [phase](#) distortion in the results. Most blind deconvolution techniques use higher-order statistics of the signals, and permit the correction of such phase distortions. We can optimize the equalizer to obtain a signal with a PSF approximating what we know about the original PSF.

### High-order statistics

Blind deconvolution algorithms often make use of [high-order statistics](#), with moments higher than two. This can be implicit or explicit.[7]